# **Identifying Locally Turbulent Vortices within Instabilities**

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### **TURBULENCE CHARACTERIZATION**

- Wide range of vortex sizes that fluctuate at different frequencies in a turbulent flow
- Laminar flow varies smoothly and predictably in space and time
- Turbulent flow exhibits a chaotic behavior
- Andrey Kolmogorov introduced statistical properties of turbulent flows
- **Turbulence** is characterized by energy transfers between these small and large eddies
- Inertial subrange describing intermediate range of eddy scales
- Energy spectrum of turbulence *E(k)* : mean turbulence kinetic energy as a function of the spatial frequency called wavenumber *k*. *E(k)* has uniform behavior in the inertial subrange.
- Energy transfer from low to high wavenumber as the form of  $E(k) \sim k^{-5/3}$  [1]
- Kinetic energy spectrum computed via a Fast Fourier transform and radial averaging [2]
- Turbulence characterization : slope of the linear regression of the energy spectrum



Kolmogorov energy cascade



Enstrophy scalar field



Shifted FFT with radial averaging over wavenumber k



#### **CFD SIMULATION CODE**

- **CFD simulation** code [3] of 2D compressible unsteady Euler equations for inviscid flows
- Approximate Riemann solver AUSM+-UP [4] to reconstruct strong discontinuities
- **Reconstruction scheme** : TENO 5 [5]
- **Periodic** boundary conditions
- **Enstrophy** defined locally as the square of the flow vorticity to capture a turbulence in 2D [6]

## Enhance the relevance of new indicators extracted with TDA regarding to traditional turbulence descriptors such as the energy cascade introduced in Kolmogorov work.

### **TOPOLOGICAL DATA ANALYSIS**

- Topological data analysis is a set of techniques [7,8] focus on structural features in data
- Established and ready to use techniques in **Paraview** [9] and **Topology ToolKit** (TTK) [10]
- Critical points on flow enstrophy represent local maxima denoting the center of vortices
- **Persistence** is used to evaluate the importance of a critical point with persistence diagrams
- Morse-Smale complex subdivides a scalar field into regions of uniform gradient flow

## **INTERPRETATIONS OF THE TURBULENCE INDICATORS**

- Morse-Smale segmentation using persistence threshold on the enstrophy scalar field
- **Classification** of the segmented vortices performed by CFD Expert
- Laminar vortices in blue and turbulent vortices in orange
- Kinetic energy spectrum calculated for each segmented vortex
- Turbulence indicator as the slope of the linear regression on the intertial subrange
- TDA segmented vortices identified as turbulent by CFD experts respect the property  $E(k) \sim k^{-5/3}$





laminar

turbulent

-1,79 turbulent

16%

9%

7%



-1,58 turbulent

5%



Vortex	Slope	Туре	diff k <sup>-5/3</sup>
6	-1,36	laminar	19%
14	-1,45	laminar	13%

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Classification of segmented vortices (laminar and turbulent) with the turbulence indicator. Thresholded Morse-Smale segmentation and kinetic energy spectrum of the vortices